

Advancements in Mathematical Model Predictive Control for Power Systems: A Lyapunov in Power Sector-Based Approach

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Abstract— These instructions give you guidelines for preparing papers for the International conference ICCSE). Use this document as a template if you are using Microsoft Office Word 6.0 or later. Otherwise, use this document as an instruction set. The electronic file of your paper will be formatted further at International Journal of Computer Theory and Engineering. Define all symbols used in the abstract. Do not cite references in the abstract. Do not delete the blank line immediately above the abstract; it sets the footnote at the bottom of this column.

Keywords- Lyapunov, Model Predictive Control, Smart Grid.

I. INTRODUCTION

The integration of informatics and mathematical sciences has emerged as a pivotal factor in the design and implementation of effective control strategies for the smart grid. By harnessing the principles of Lyapunov theory, this innovative approach has demonstrated remarkable advancements in enhancing the stability, robustness, and overall performance of power systems.

The smart grid represents a modern and intelligent power distribution network that relies on advanced technologies and communication systems to optimize energy generation, transmission, and consumption. To ensure the smooth operation of this complex network, it is imperative to develop control strategies that can adapt to dynamic changes, mitigate uncertainties, and maintain grid stability.

Informatics, encompassing various disciplines such as computer science, data analytics, and artificial intelligence, provides the tools and methodologies to process and analyze vast amounts of data generated by the smart grid. By leveraging these techniques, valuable insights can be extracted, enabling effective decision-making and control.

Mathematical sciences, on the other hand, offer a solid foundation for modeling, analyzing, and optimizing power systems. Lyapunov theory, a branch of mathematics concerned with stability and control, has proven to be particularly valuable in the context of the smart grid. By employing Lyapunov-based control strategies, it becomes possible to ensure stability, robustness, and performance improvement in power systems.

The principles of Lyapunov theory provide a rigorous framework for assessing the stability of a system and designing control strategies that guarantee convergence to desired operating points. By utilizing this theory, control algorithms can be developed to regulate power flow, manage

voltage levels, and handle contingencies in real-time, ensuring the stable and reliable operation of the smart grid.

II. LITERATURE REVIEW

In [2], the article proposed an interlinking converter based on model predictive control to maintain a smooth output from a photovoltaic system by controlling the state of charge in the energy storage. The control strategy ensured power balance and supported voltage variation levels through injected reactive power.

The review paper [4] also focused on model predictive control in networked microgrids, highlighting its applications in grid-level control, voltage regulation, frequency control, power flow management, and economic optimization. It emphasized the use of dynamically upgraded model predictive control in a centralized energy management system to achieve technical goals related to power quality and continuous power flow.

In [5], the review paper discussed the advantages of model predictive control over various modeling methods for grid-connected and islanded systems. It highlighted the strengths, weaknesses, and different approaches to handling uncertainties in microgrids. The article also proposed robust predictive control algorithms for modern energy systems, particularly with a focus on increasing renewable energy resources.

Lastly, [6] proposed a consensus-based energy management system using model predictive control for battery energy storage systems and distributed renewable energy source units. The system employed individual controllers to operate in grid-forming or grid-feeding configurations, based on the generated power, load power, and energy storage's level of charge. The energy management system determined the mode of power flow accordingly.

The study presented in [1] introduced a power management strategy for standalone PV/battery systems using model predictive control. The controller was designed to effectively manage power by switching the operation of the PV system between power-curtailed mode and maximum power point tracking mode, while minimizing transients during disturbances.

Lastly, [6] proposed a consensus-based energy management system using model predictive control for battery energy storage systems and distributed renewable energy source units. The system employed individual controllers to operate in grid-forming or grid-feeding configurations, based on the generated power, load power, and energy storage's level of charge. The energy management system determined the mode of power flow accordingly.

The review paper [3] discussed the applications of model predictive control in networked microgrids, emphasizing its effectiveness in grid-level control, voltage regulation, frequency control, power flow management, and economic optimization. The control model presented in this paper was considered as a potential replacement for conventional approaches, offering benefits such as managing power flow, optimizing economics, and controlling frequency and voltage.

III. OVERVIEW OF THE SMART GRID AND ITS CHALLENGES

The smart grid is an advanced power distribution network that incorporates modern technologies and communication systems to optimize energy generation, transmission, and consumption. It aims to enhance grid reliability, efficiency, and sustainability. However, the integration of renewable energy sources, electric vehicles, and decentralized generation poses significant challenges to the stability and control of the smart grid. These challenges include managing fluctuations in power supply, maintaining grid stability, and ensuring efficient energy utilization.

To address the challenges posed by the smart grid, advanced control techniques are essential. Traditional control methods may not be sufficient to handle the dynamic and complex nature of the smart grid [9]. Advanced control techniques can provide real-time monitoring, decision-making, and control capabilities to ensure the reliable and optimal operation of the grid.

By using Lyapunov-based MPC, each component of the smart grid can have its own control algorithm that optimizes its operation based on local measurements and objectives while ensuring stability and coordination with other components. This enables the smart grid to achieve efficient and robust operation, even in the presence of uncertainties and disturbances. The Lyapunov function provides a measure of the system's stability, allowing each component to make decisions that collectively result in a stable and optimal grid operation.

Grid Complexity

One of the challenges in utilizing Lyapunov-based MPC in grid complexity is the variability of electricity demand. The demand for electricity can fluctuate significantly due to factors such as time of day, weather conditions, and economic activities. These variations in demand pose challenges for accurate prediction and control of the grid. Lyapunov-based MPC algorithms need to account for demand variability and adapt their control strategies accordingly to ensure grid stability and optimal performance.

Another challenge in utilizing Lyapunov-based MPC in grid complexity is the integration of advanced control techniques. As the power grid becomes more complex with the integration of renewable energy sources, energy storage systems, and distributed generation, advanced control techniques are required to effectively manage and control the grid [10]. Lyapunov-based MPC can provide stability guarantees and performance optimization, but integrating it with other advanced control techniques, such as optimal power flow algorithms or hierarchical control structures, can be challenging. The coordination and interaction between different control techniques need to be carefully designed and implemented to ensure the overall stability and performance of the grid.

Intermittency of Renewables

The intermittent nature of renewable energy sources, such as solar and wind, poses challenges in utilizing Lyapunov-based MPC. The availability of renewable energy generation depends on weather conditions and natural resources, which can vary over time. This intermittency introduces uncertainties in the power generation, making it challenging to predict and control the grid effectively. Lyapunov-based MPC algorithms need to account for the intermittent nature of renewables and incorporate robust control strategies to ensure grid stability and reliable operation while maximizing the utilization of renewable energy.

The integration of renewable energy sources into the power grid requires supportive regulatory frameworks and policies. However, the development and implementation of such regulations and policies can be challenging. Different jurisdictions may have varying regulations and policies regarding renewable energy integration, grid connection standards, and incentive mechanisms [11]. These regulatory and policy challenges can affect the deployment and utilization of Lyapunov-based MPC in managing the intermittency of renewables. Collaboration between policymakers, grid operators, and technology developers is crucial to address these challenges and create an enabling environment for the effective utilization of Lyapunov-based MPC.

Data Management

Grid resilience refers to the ability of the power grid to withstand and recover from disruptions, including natural disasters, cyber-attacks, and equipment failures. In the context of utilizing Lyapunov-based MPC in data management, grid resilience is a significant challenge [12]. The increasing reliance on data for grid monitoring, control, and optimization introduces vulnerabilities to cyber threats and data breaches. Protecting the integrity, confidentiality, and availability of grid data is essential to ensure the effectiveness and security of Lyapunov-based MPC algorithms. Robust cybersecurity measures and protocols need to be implemented to mitigate the risks and ensure grid resilience

The increasing digitization and connectivity of the power grid expose it to cybersecurity threats. Lyapunov-based MPC relies on accurate and reliable data for control and optimization. However, cyber-attacks targeting the grid's data infrastructure can compromise the integrity and reliability of the data, leading to incorrect control decisions and potential grid instability. Protecting against cybersecurity threats, such as unauthorized access, data manipulation, and denial-of-service attacks, is crucial in utilizing Lyapunov-based MPC effectively. Robust cybersecurity measures, including encryption, authentication, and intrusion detection systems, need to be implemented to safeguard the grid's data infrastructure.

Figure 2 gathers areas with needed aspects of smart grid that can be solve using the application of Lyapunov-based Model Predictive Control (MPC).

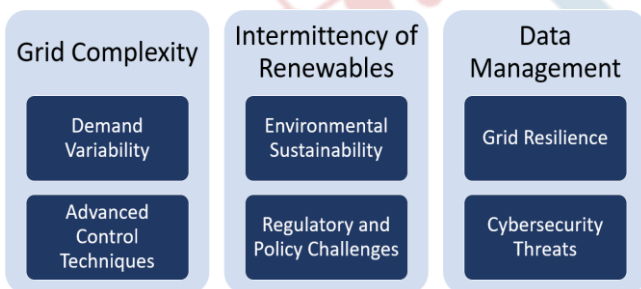


Figure 1. Challenges in smart grid in areas

IV. ENHANCING STABILITY, ROBUSTNESS, AND PERFORMANCE

Grid stability is crucial for maintaining a reliable power supply and preventing blackouts. Mathematical models represent the dynamics of the grid and aid in stability analysis. Robust control strategies adapt to uncertainties and disturbances, optimizing resources for efficient grid operation. Mathematical optimization techniques allocate resources optimally. Performance metrics such as voltage regulation, frequency control, and power quality evaluate grid performance. Mathematical techniques are used for fault detection and isolation in the grid.

Mathematical models play a vital role in representing the dynamics of the grid and aiding in stability analysis. These models capture the behavior of various components in the power system, such as generators, transmission lines, transformers, and loads. By mathematically describing the interactions between these components, models can simulate the behavior of the grid under different operating conditions and disturbances.

Grid stability is of utmost importance in maintaining a reliable power supply and preventing blackouts. It refers to the ability of an electrical power grid to maintain a steady and balanced operation despite disturbances and fluctuations in power generation, consumption, and transmission [13]. Grid stability ensures that the supply of electricity matches the demand, and any deviations are quickly corrected to avoid disruptions in power delivery.

Robust control strategies are designed to adapt to uncertainties and disturbances in the grid, ensuring stability and reliable operation. These strategies account for variations in power generation, load demand, and other factors that can affect the grid's performance. Mathematical optimization techniques are employed to allocate resources optimally and ensure efficient grid operation. These techniques help grid operators make decisions that minimize costs, maximize power system reliability, and improve overall performance.

Several key performance metrics are used to evaluate the operation and stability of the power grid. These metrics provide insights into the quality of power supply, the ability to maintain voltage and frequency within acceptable limits, and the overall reliability of the grid. Mathematical techniques are used for fault detection and isolation in the power grid. These techniques analyze system measurements and data to identify faults, such as short circuits or equipment failures, and locate their precise locations.

Mathematical models play a crucial role in enhancing grid stability, robustness, and performance. They provide a systematic and quantitative approach to understanding and optimizing various aspects of the power grid. Mathematical models play a crucial role in enhancing grid stability, robustness, and performance. They provide a systematic and quantitative approach to understanding and optimizing various aspects of the power grid. The figure 1 shows mathematical models importance in grid optimization.

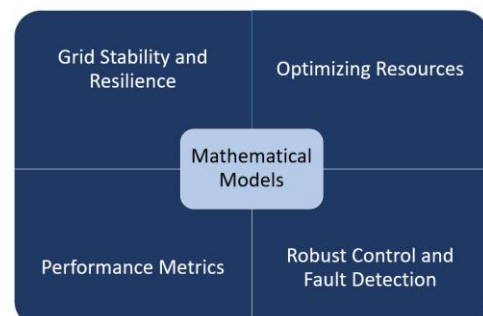


Figure 2. Methods for grid optimization

V. COMBINING MPC AND LYAPUNOV THEORY FOR POWER SYSTEMS CONTROL

Model Predictive Control (MPC) is a control strategy that uses mathematical models of the system to predict its future behavior and optimize control actions accordingly. MPC considers constraints, objectives, and predictions of system behavior to determine the optimal control inputs. It has been widely applied in various fields, including power systems, due to its ability to handle complex systems with constraints and uncertainties.

Lyapunov theory is a mathematical framework used in control theory to analyze the stability of dynamical systems. It provides a rigorous method to assess the stability of a system by analyzing the properties of a Lyapunov function. Lyapunov theory enables the design of control strategies that guarantee stability and convergence to desired operating points.

The combination of MPC and Lyapunov theory offers a powerful control framework for power systems in the smart grid. By utilizing Lyapunov theory, stability guarantees can be incorporated into the MPC formulation [14]. This ensures that control actions are not only optimized but also maintain system stability.

MPC can utilize real-time measurements and predictions to make control decisions that consider system constraints, load variations, and renewable energy availability. By continuously updating control actions based on current system states, MPC can adapt to changing conditions and optimize system performance.

The incorporation of Lyapunov theory in the MPC framework allows for the design of control algorithms that ensure stability and convergence to desired operating points. Lyapunov-based control strategies provide robustness against uncertainties and disturbances, enhancing the overall performance and reliability of power systems in the smart grid.

By combining the strengths of MPC and Lyapunov theory, a comprehensive control framework can be developed for power systems in the smart grid. This framework enables the effective management of energy resources, the integration of renewable energy sources, and the maintenance of grid stability, ultimately leading to a more efficient and sustainable smart grid.

VI. POSSIBLE APPLICATION FOR COORDINATED CONTROL SYSTEMS

The Lyapunov-based Model Predictive Control (MPC) approach has several potential applications in the smart grid domain. It can be utilized for demand response, energy management, grid integration of electric vehicles, and decentralized control strategies. Using cooperation of MPC and Lyapunov algorithm it is easy to respond demand, manage energy, integrate electric vehicles to grid, and strategy decentralized control.

Demand response refers to the ability to adjust electricity consumption in response to changes in electricity prices or grid conditions. The Lyapunov-based MPC approach can be used to develop control strategies that optimize demand response in the smart grid.

By using Lyapunov-based MPC, the smart grid can effectively manage and optimize the demand response process. The Lyapunov function provides a measure of the system's stability and performance, allowing the control algorithm to adjust the electricity consumption in real-time based on the grid conditions and price signals. This can help balance the supply and demand of electricity, reduce peak loads, and improve the overall efficiency of the grid.

Energy management in the smart grid involves optimizing the allocation and utilization of energy resources to meet the demand while minimizing costs and maintaining grid stability. The Lyapunov-based MPC approach can be applied to develop energy management strategies that ensure efficient and reliable operation of the grid.

With the Lyapunov-based MPC approach, the smart grid can dynamically optimize energy generation, storage, and consumption based on real-time information about the grid conditions, renewable energy availability, and demand patterns. The Lyapunov function can be used to formulate an objective function that captures the system's stability and performance, allowing the control algorithm to make optimal decisions for energy management.

The integration of electric vehicles (EVs) into the smart grid presents both challenges and opportunities. The Lyapunov-based MPC approach can be employed to address these challenges and exploit the opportunities for grid integration of EVs.

Lyapunov-based MPC can be used to develop control strategies that optimize the charging and discharging of EVs based on grid conditions, electricity prices, and user preferences. This enables the smart grid to effectively manage the charging and discharging of EVs, avoid overloading the grid, and maximize the utilization of renewable energy sources [15]. It also allows for the integration of EVs as flexible energy storage devices that can provide ancillary services to the grid, such as frequency regulation and peak shaving.

Decentralized control strategies aim to distribute control and decision-making capabilities across various components of the smart grid. The Lyapunov-based MPC approach can be employed to develop decentralized control strategies that enhance the overall performance and reliability of the grid.

Figure 3 shows areas in smart grid where Lyapunov-based MPC can be applied.

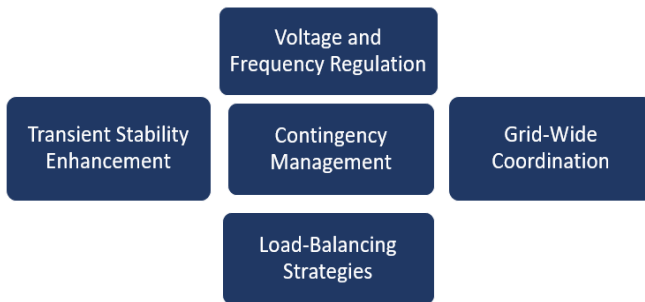


Figure 3. Possible application for Lyapunov-based Model Predictive Control

VII. CONCLUSIONS

The application of Lyapunov-based Model Predictive Control (MPC) techniques in power systems can contribute to the growing body of knowledge in informatics and mathematical sciences for the smart grid. This research provides valuable insights and a solid foundation for researchers, practitioners, and industry experts to further explore and implement Lyapunov-based MPC techniques in power systems.

By leveraging Lyapunov-based MPC, power system operators can achieve more efficient, reliable, and sustainable operation of the smart grid. The research conducted in this area can help optimize demand response, energy management, grid integration of electric vehicles, and decentralized control strategies.

The insights gained from this research can inform the development of advanced control algorithms and decision-making strategies that take into account real-time grid conditions, renewable energy availability, electricity prices, and user preferences. By integrating Lyapunov-based MPC techniques, the smart grid can dynamically adjust electricity consumption, optimize energy generation and storage, manage the charging and discharging of electric vehicles, and enhance the overall performance and stability of the grid.

Furthermore, the research in informatics and mathematical sciences for the smart grid can foster collaborations between academia, industry, and government agencies. This collaboration can lead to the implementation of innovative solutions and the adoption of Lyapunov-based MPC techniques in real-world power systems. The findings from this research can also serve as a basis for developing standards and guidelines for the application of Lyapunov-based MPC in the smart grid domain.

Overall, the research on Lyapunov-based MPC techniques in power systems contributes to the advancement of informatics and mathematical sciences for the smart grid. It provides valuable insights and a solid foundation for further exploration and implementation of these techniques, leading to more efficient, reliable, and sustainable operation of the smart grid.

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